חAmibia university
OF SCIEПCE AחD TECHחOLOGY

## FACULTY OF MANAGEMENT SCIENCES

DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

| QUALIFICATION: BACHELOR OF TECHNOLOGY IN ECONOMICS |  |
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| QUALIFICATION CODE: 12BECO | LEVEL: 7 |
| COURSE CODE: AME311S | COURSE NAME: APPLIED MATHEMATICAL <br> ECONOMICS |
| SESSION: JULY 2019 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SUPPLEMENTARY/ SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINER(S) |  |
|  | MR EDEN TATE SHIPANGA |
| MODERATOR: | PROF T. SUNDE |

## INSTRUCTIONS

1. Answer ALL the questions.
2. Write clearly and neatly.
3. Number the answers clearly.

## PERMISSIBLE MATERIALS

1. PEN,
2. PENCIL
3. CALCULATOR

THIS QUESTION PAPER CONSISTS OF 2 PAGES (Including this front page)

## Question 1 [25 Marks]

Consider the following microeconomic model.

$$
\left.\begin{array}{ll}
Q_{d}=D\left(P, Y_{0}\right) & {\left[D_{P}<0 ;\right.} \\
\left.D_{Y_{0}}>0\right] \\
Q_{s}=D\left(P, T_{0}\right) & {\left[S_{P}>0 ;\right.}
\end{array} S_{T_{0}}<0\right] ~ \$
$$

Where $Y_{0}$ is income and $T_{0}$ is the tax on the commodity.
Analyse the comparative statics of the model to find the effect of change in Income and Tax on the equilibrium Q and P ?

## Question 2 [25 Marks]

1. Use the Jacobian to test for functional dependence in the following system of equations

$$
\begin{aligned}
& y_{1}=6 x_{1}+4 x_{2} \\
& y_{2}=7 x_{1}+9 x_{2}
\end{aligned}
$$

5 marks
2. Maximize utility $u=x y+x$, subject to the budget constraint $6 x+2 y=110$ by a) finding the critical values $\bar{x}, \bar{y}$ and $\bar{\lambda}, \mathrm{b}$ ) use the Hessian bordered.

20 marks

## Question 3 [25 Marks]

In a three-industry economy, it is known that industry I uses 20 cents of its own product, 10 cents of commodity III and 60 cents of commodity II to produce a dollar's worth of commodity I. Industry II uses 10 cents of its own product, 30 cents of commodity III and 50 cents of commodity I to produce a dollar's worth of commodity II. While industry III uses none of its own product and commodity I; but uses 20 cents of commodity II in producing a dollar's worth of commodity III. The open sector demands $\mathrm{N} \$ 1,000$ billion of commodity I, N $\$ 2,000$ billion of commodity II and 500 billion of commodity III
a) Write out the input matrix, and the specific input matrix equation for this economy.

10 marks
b) Find the solution output levels by Cramer's rule.

## Question 4 [25 Marks]

1. Given the marginal propensity to consume $C^{\prime}(Y)=8+0.1 Y^{1 / 2}$ and information that $C=Y$ when $Y=100$, find the consumption function $C(Y)$.

10 marks
2. Evaluate the following

$$
\text { a) } \int_{0}^{4}\left(\frac{1}{1+3 x}+2 x\right) d x \text { where } x \neq-1
$$

b)

$$
\int_{0}^{4}\left(2 x^{3}-1\right)^{2}\left(6 x^{2}\right) d x .
$$

15 marks

